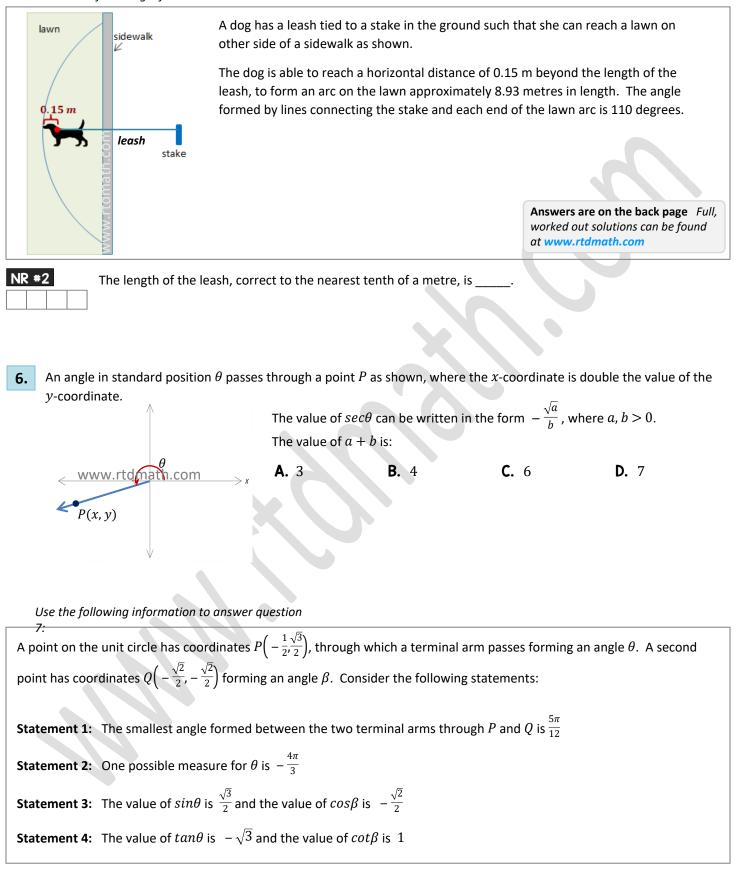
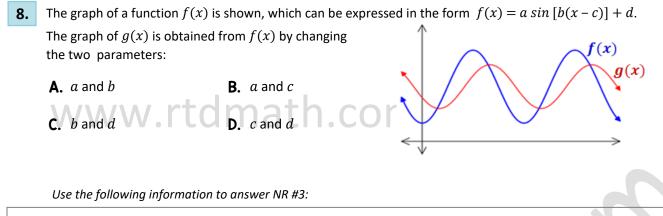


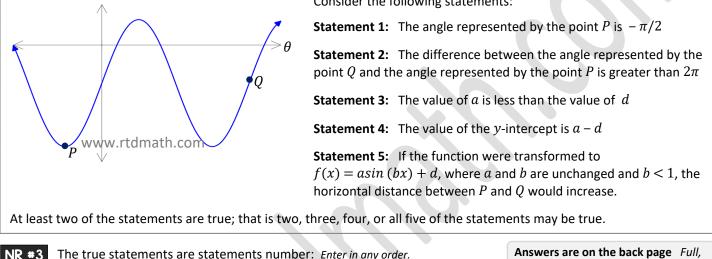
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7.



The graph shown models a sinusoidal function in the form f(x) = asinx - d, where a > 0 and d > 0. The point P is at a minimum. Consider the following statements:



 R #3
 The true statements are statements number: Enter in any order.

Answers are on the back page Full, worked out solutions can be found at www.rtdmath.com

**9.** A sinusoidal function has an equation  $y = 5sin (4x + \pi)$ . The value of the **period** and the **horizontal phase shift** are, respectively:

**A.**  $\frac{\pi}{2}, \frac{\pi}{4}$  **B.**  $\frac{\pi}{2}, \pi$  **C.** 4,  $\pi$  **D.** 4,  $\frac{\pi}{4}$ 

NR #4

A sinusoidal function has an f

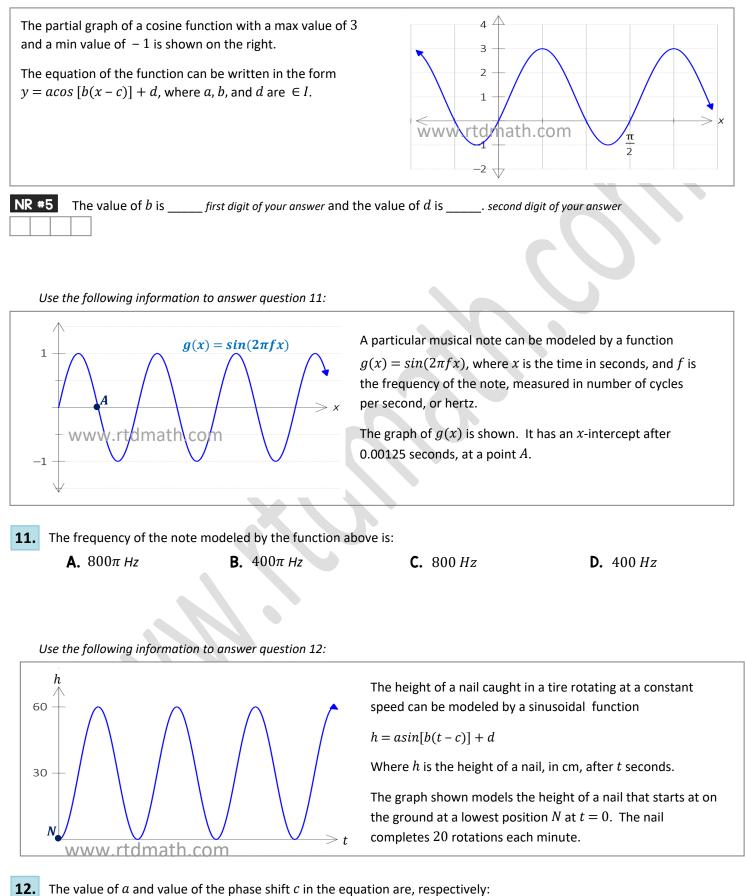
The **period** of the resulting graph, correct to the nearest whole number, is a two-digit number *ab* (*a and b are the first two digits of your answer*)

The **maximum value** of the function, correct to the nearest tenth, is c.d (c and d are the last two digits of your answer)

The values of *a*, *b*, *c* and *d* are:\_\_\_\_\_

**10.** The function f(x) = tan(4x) has a domain, where  $n \in I$ , of:

**A.**  $x \neq \frac{\pi}{4} + \frac{n\pi}{2}$  **B.**  $x \neq \frac{\pi}{4} + \frac{n\pi}{4}$  **C.**  $x \neq \frac{\pi}{8} + \frac{n\pi}{2}$  **D.**  $x \neq \frac{\pi}{8} + \frac{n\pi}{4}$ 

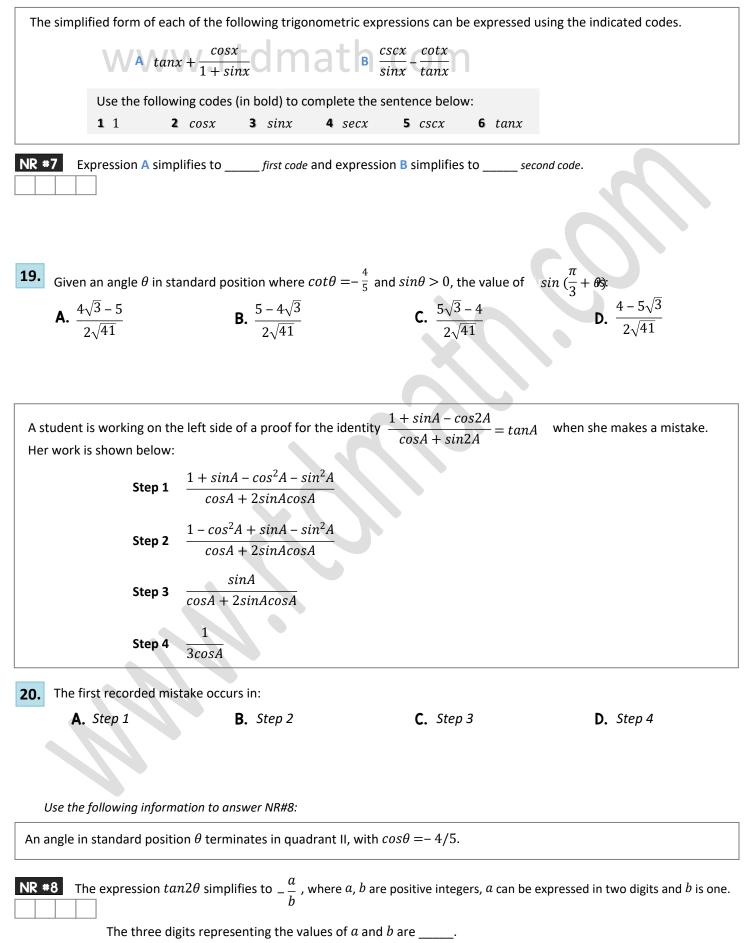


**13.** Which of the following steps could lead to a correct solution of the equation  $2\cos^2\theta + 3\cos\theta - 2 = 0$ ?

**A.** 
$$\cos\theta = \frac{1}{2} \operatorname{or} \cos\theta = -2$$
 **B.**  $\cos\theta = \frac{1}{2} \operatorname{or} \cos\theta = -1$  **C.**  $\cos\theta = \frac{-1}{2} \operatorname{or} \cos\theta = 2$  **D.**  $\cos\theta = \frac{-1}{2} \operatorname{or} \cos\theta = 1$ 

**14.** The solution, on 
$$\{0 \le x \le 2\pi\}$$
, to  $3\csc^2\theta - 4 = 0$  is  $\theta$  equal to:  
**A.**  $\frac{\pi}{3'3}$ 
**B.**  $\frac{\pi}{3'3}\frac{2\pi 4\pi}{3'3}\frac{5\pi}{3'3}$ 
**C.**  $\frac{\pi}{6'}\frac{5\pi}{6}$ 
**D.**  $\frac{\pi}{6'}\frac{5\pi}{6'}\frac{7\pi}{6'}\frac{11\pi}{6}$ 
**15.** A general solution of the equation  $\sec^2 x - \sec x - 2 = 0$ , where  $n \in I$  is:  
**A.**  $x = \frac{\pi}{3}n$ 
**C.**  $x = \frac{\pi}{3}n + \frac{2\pi n}{3}$ 
**B.**  $x = \frac{\pi}{3} + 2\pi n$ ,  $x = \pi n$ 
**D.**  $x = \frac{\pi}{3} + 2\pi n$ ,  $x = 2\pi n$ 
**16.** The solution to the equation  $\log_2(\tan x) + \log_2(\cos x) + 1 = 0$ , where  $\{0 \le x \le 2\pi\}$  is:  
**A.**  $x = \frac{\pi}{6'}\frac{5\pi}{6'}\frac{\pi}{2}$ 
**B.**  $x = \frac{7\pi}{6'}\frac{11\pi}{6}$ 
**C.**  $x = \frac{\pi}{6'}\frac{5\pi}{6}$ 
**D.**  $x = \frac{7\pi}{6'}\frac{11\pi}{6'}\frac{\pi}{2}$ 
**IVE G The** exact value of the trig ratio  $\cos(\frac{\pi}{12})$  can be determined to be an irrational expression in the form  $\frac{\sqrt{a} - \sqrt{b}}{c}$ 
where  $a, b, c$  are positive integers.  
The value of  $a$  is first digit, the value of  $b$  is second digit and the value of  $c$  is since  $d$  is  $\frac{3}{\sqrt{34}}$ 
**B.**  $-\frac{3}{\sqrt{34}}$ 
**C.**  $\frac{5}{\sqrt{34}}$ 
**D.**  $\frac{5}{\sqrt{34}}$ 
**D.**  $\frac{5}{\sqrt{34}}$ 
**13.** The non-permissible values of the expression  $\frac{\tan x}{1 + \sin x}$  can be best written, where  $n \in I$ , as:  
**A.**  $x = \frac{3\pi}{2} + 2\pi n$ 
**B.**  $x = \pi n$ ,  $x = \frac{3\pi}{2} + 2\pi n$ 
**C.**  $x = \frac{\pi}{2} + \pi n$ 
**D.**  $x = \pi n$ ,  $x = \frac{\pi}{2} + 2\pi n$ 

Use the following information to answer NR#7:



# PART 2 - Written Response

Use the following information to answer WR#1:

An angle in standard position $\theta$ passes through a point $P(-5, 1)$ and a second angle in standard position $\beta$ passes	j
through a point $Q(-3, -4)$ .	

#### \* Written Response Question 1

• Fully **sketch** each angle in the correct quadrant labeling all sides of the triangle, and **determine** the value of each angle, correct to the nearest degree. (3 marks)

• **Determine** the exact value of  $sin(\theta + \beta)$ , written in the form  $\frac{p}{q}$  (2 marks)

## \* Written Response Question 2

• Using a trigonometric identity, **simplify** the equation  $2sin^2x - cosx - 1 = 0$  to express in terms of one trig function, where the lead coefficient is positive. (2 marks)

• Algebraically solve the resulting equation on  $\{0 \le x < 2\pi\}$ , and state a general solution. (3 marks)

### \* Written Response Question 3

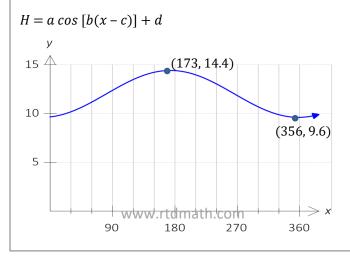
• **Prove** the equation  $\frac{cscx cosx}{tanx + cotx} = cos^2 x$  is an identity using an algebraic approach. (3 marks)

• Determine each of the possible non-permissible values, in radians. (2 marks)

In San Diego, California the number of hours of daylight follows a sinusoidal pattern where the maximum hours of sunlight is 14.4 hours on day 173 (June 27<sup>th</sup>), and the minimum hours of sunlight is 9.6 hours on day 356 (Dec 22<sup>nd</sup>).

The function below is for a particular leap year of 366 days.

The hours of sunlight (H) can be modeled as a cosine function of day number (x):



#### \* Written Response Question 4

• **Determine** the values of a, b, c, and d in the equation  $H = a \cos[b(x - c)] + d$  (3 marks)

• The daily high temperature in San Diego can be modeled by the function T = 5.1sin [0.524(d - 2.75)] + 23.9, where T is the temperature in degrees Celsius, and m is the number of months from the start of the year.

Use a graphing approach to **determine** the approximate total number of months, correct to the nearest tenth, where the daily high temperature would be above  $26^{\circ}$ C. (2 marks)

• A function of similar form to the last bullet is constructed for Calgary Alberta, where the temperatures are much cooler. **Explain** which of the two parameters *a*, *b*, *c*, and *d* would be different, and how. **Justify** your reasoning. (Note, on the actual diploma exam each WR question will have exactly two bullets)



For full, worked-out solutions (as well as other practice materials) visit www.rtdmath.com) This practice exam was produced by RTD Learning for not-for-profit use by Alberta students and teachers

## **Multiple Choice**

1. D 2. B 3. A 4. C 5. C 6. D 7. C 8. B 9. A 10. D 11. D
12. A 13. A 14. B 15. C 16. C 17. D 18. C 19. B 20. A
Numerical Response
<b>1.</b> 3.5 <b>2.</b> 4.5 <b>3.</b> 125 <b>4.</b> 5281 <b>5.</b> 41 <b>6.</b> 264 <b>7.</b> 41 <b>8.</b> 247
Written Response
<b>1.</b> First bullet $\theta = 169^{\circ} \beta = 233^{\circ}$ Second bullet $\frac{17}{5\sqrt{26}}$
<b>2.</b> First bullet $2\cos^2 x + \cos x - 1 = 0$ Second bullet $x = \frac{\pi}{3}, \pi, \frac{5\pi}{3}$ (any order) $x = \frac{\pi}{3} + \frac{2\pi}{3}n$ $n \in I$ (general sol.)
<b>3.</b> First bullet See full solutions on <u>www.rtdmath.com</u> Second bullet $x \neq \frac{\pi}{2}n$ , $n \in I$
<b>4.</b> First bullet $a = 2.4$ , $b = \frac{\pi}{183}$ , $c = 173$ , $d = 12$ Second bullet <b>4.4</b> total months above 26°C.
Third bullet <b>a</b> would be <b>higher</b> , as the range of Calgary temperatures (between min and max) would be greater

 $m{d}$  would be **lower**, as the median temperature for Calgary (represented by  $m{d}$ ) would be lower

Also.... (not needed in your answer)

**b** would be **unchanged**, as the period for each city would be the same (12 months). Similarly, **c** would be essentially unchanged, as the number of months after which the min / max temperature occurs would be approximately the same as both cities are in the northern hemisphere.